## Deriving Transition Probabilities for Decision Models

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D HEASRAD

## Transition probabilities drive the decision model

- Probability of moving from one health state to another (state-transition model)
- Probability of experiencing an event (discrete-event simulations)


## Goal

- (Transition) probabilities are the engine to a decision model
- You will often derive these probabilities from literature-based inputs
- Learn when and how you can do this


## Acknowledgements

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- Member, National Academy of Medicine
- Rita Popat, PhD

Clinical Associate Professor, Division of Epidemiology, Stanford University School of Medicine

## Probabilities in a Decision Model

- You have a cost-effective model, now you need inputs for your transition probabilities



## Probabilities in a Decision Model

- Does not have to be 2 drugs - can be any strategies



## Probability Inputs



## Ways to derive model inputs

- Obtain existing data from a single study
- Synthesizing existing data from multiple studies
- Meta-Analysis
- Mixed Treatment Comparisons
- Meta-Regression


## USING EXISTING DATA FROM A SINGLE STUDY

## Plucking inputs from the literature

- If you are extremely lucky, you will read a journal article that will have exactly the type of information you need.
- The vast majority of people are not extremely lucky.
- Modify existing literature to derive your model inputs


## Using inputs from the literature

- Many types of inputs are available from the literature
- Probability (risk)
- Rate (mortality)
- Relative Risk
- Odds Ratio
- Risk Difference
- Mean
- Median
- We need data in the form of probabilities for use in a model


## What do these inputs mean?

| Statistic | Evaluates | Range |
| :---: | :---: | :---: |
| Probability/Risk (aka Incidence Proportion) | \# of events that occurred in a time period <br> \# of people followed for that time period | 0-1 |
| Rate | \# of events that occurred in a time period <br> Total time period experienced by all subjects followed | 0 to $\infty$ |
| Relative Risk (aka Risk Ratio) | $\frac{\text { Probability of outcome in exposed }}{\text { Probability of outcome in unexposed }}$ | 0 to $\infty$ |
| Odds | $\frac{\text { Probability of outcome }}{1-\text { Probability of outcome }}$ | 0 to $\infty$ |
| Odds Ratio | $\frac{\text { Odds of outcome in exposed }}{\text { Odds of outcome in unexposed }}$ | 0 to $\infty$ |
| Risk Difference | Difference in risk (probability) of event amongst exposed and unexposed | -1 to 1 |
| Survival Curve | Point $=$ $\#$ of people who are alive at time $t \mid$ being alive at time $t-1$ | 0 to n |
| Mean | $\frac{\text { Sum of all observations }}{\text { Total \# of observations }}$ | - $\infty$ to $\infty$ |

## Comparative, Non-Comparative Data

| Statistic | Evaluates | Type of Data |  |
| :---: | :---: | :---: | :---: |
| Probability/Risk | \# of events that occurred in a time period <br> \# of people followed for that time period | Non-Comparative |  |
| Rate | $\frac{\# \text { of events }}{\text { Total time period experienced by all subjects followed }}$ | Non-Comparative |  |
| Odds | Probability of outcome <br> $\overline{1 \text { - Probability of outcome }}$ | Non-Comparative |  |
| Odds Ratio | $\frac{\text { Odds of outcome in exposed }}{\text { Odds of outcome in unexposed }}$ | Comparative |  |
| Relative Risk (aka Risk Ratio) | $\frac{\text { Probability of outcome in exposed }}{\text { Probability of outcome in unexposed }}$ | Comparative | Transform to Non-Comparative Data |
| Risk Difference | Difference in risk (probability) of event amongst exposed and unexposed | Comparative |  |
| Survival Curve | Point = \# of people who are alive at time $t$ \| being alive at time t - 1 | Non-Comparative |  |
| Mean | Sum of all observations <br> Total \# of observations | Non-Comparative |  |

## Inputs for a decision model require non-comparative data:

Ex. 1) Probability of controlled diabetes with Drug A as the first input
2) Probability of controlled diabetes with Drug B as the second input

## Using probabilities from the literature

- Literature-based probability may not exist for your time frame of interest
- Transform this probability to a time frame relevant for your model
- Example:
- 6-month probability of controlled diabetes is reported in the literature
- Your model has a 3-month cycle length
- You need a 3-month probability


## Probabilities cannot be manipulated easily

- Cannot multiply or divide probabilities
- $100 \%$ probability at 5 years does NOT mean a $20 \%$ probability at 1 year
- $30 \%$ probability at 1 year does NOT mean a $120 \%$ probability at 4 years


## Probabilities and Rates

- Rates can be mathematically manipulated -- added, multiplied, etc.
- Probabilities cannot
- To change time frame of probability: Probability $\rightarrow$ Rate $\rightarrow$ Probability
- Note: Assumes the event occurs at a constant rate over a particular time period


## Rates versus probabilities

- In a rate, you care when the event happened - this changes the rate (but not the probability)

- The rate of death is $3 /(3+4+1+2)=3 / 10$ :
- 3 per 10 person-years, 0.3 per person-year
- The probability of death is $3 / 4$ :
- 75\%


## Rates versus probabilities, 2




Rate of death $=0.3$ per person-year $3 /(3+4+1+2)=3 / 10$
Probability of death $=75 \%$

$$
=3 / 4
$$

Rate of death $=0.5$ per person-year

$$
3 /(0.5+4+1+0.5)=3 / 6
$$

Probability of death $=75 \%$
$=3 / 4$

## Example- Question

Calculate the rate of death and the probability of death from the following data:

Rate: \# of events/\# of person-years<br>Probability: \# of events/\# of persons followed



## Example- Answer

Calculate the rate of death and the probability of death from the following data:


Rate of death $=\mathbf{0 . 3 7 5}$ per person-year

$$
3 /(2+3+1+2)=3 / 8
$$

Probability of death $=\mathbf{7 5 \%}$
$=3 / 4$

## Probability-Rate Conversions

- Probability to rate

$$
\text { Rate }=\frac{-\ln (1-p)}{t}
$$

- Rate to probability

$$
\text { Probability }=1-\exp ^{(-r t)}
$$

$$
\begin{aligned}
& p=\text { probability } \\
& t=\text { time } \\
& r=\text { rate }
\end{aligned}
$$

## Example

- 3-year probability of controlled diabetes is $60 \%$
- What is the 1-year probability of controlled diabetes?
- Assume incidence rate is constant over 3 years:
- Rate $=\frac{-\ln (1-p)}{t}$
$-=\frac{-\ln (1-0.6)}{3}=0.3054$
- Probability $=1-\exp ^{(-r t)}$

$$
\begin{aligned}
=1-e^{(-0.3054 \times 1)} & =0.2632 \\
& =26 \%
\end{aligned}
$$

## Question

- $30 \%$ of people have controlled diabetes at 5 years.
- What is the 1 -year probability of controlled diabetes?
- Probability to rate

$$
\text { Probability }=1-\exp ^{(-r t)}
$$

- Rate to probability

$$
\text { Rate }=\frac{-\ln (1-p)}{t}
$$

$$
\begin{aligned}
& p=\text { probability } \\
& t=\text { time } \\
& r=\text { rate }
\end{aligned}
$$

## Answer

- A 5-year probability of $30 \%$ is a 1 -year probability of $\mathbf{6 . 8 9 \%}$.
- Equations:
- Rate $: \frac{-\ln (1-0.30)}{5}=0.0713$
- Probability : $1-e^{(-0.0713 \times 1)}=6.89 \%$


## Confidence Intervals around Derived Probabilities

- Need to include the uncertainty around your point estimate (more in a future lecture)
- 95\% Confidence Interval
- Use the same prob $\rightarrow$ rate $\rightarrow$ prob equations to convert the upper and lower bounds of the CI

| Controlled Diabetes (5 year) | $30 \%$ |
| :--- | :---: |
| Controlled Diabetes (Annual Rate) | 0.0713 |
| Controlled Diabetes (Annual Probability) | 0.0689 |


| $95 \% \mathrm{CI}$ (reported, 5 years) | $25 \%-35 \%$ |
| :--- | :--- |


| Lower bound (5-year) | $25 \%$ |
| :--- | :---: |
| Lower bound (Annual rate) | 0.0575 |
| Lower bound (Annual prob) | $\mathbf{0 . 0 5 5 9}$ |$\quad$| Upper bound (5 year) | $35 \%$ |
| :--- | :---: |
| Upper bound (Annual rate) | 0.0862 |
| $\quad$ Upper bound (Annual prob) | $\mathbf{0 . 0 8 2 5}$ |

6.89\% (5.59\%-8.25\%)

## Converting to Probabilities?

| Statistic |  |  |
| :--- | :--- | :--- |
| $\checkmark$ | Probability/Risk <br> (aka Incidence Proportion) | Yes (it is already one, but use rates to convert the time period to which <br> they apply) |
| $\checkmark$ | Rate | Yes |
|  | Relative Risk (aka Risk Ratio) |  |
|  | Odds |  |
| Odds Ratio |  |  |
| Risk Difference (x-y=z) |  |  |
| Survival Curve |  |  |
| Mean |  |  |

## In the beginning...

there were 2 by 2 tables:

|  | Outcome - Yes | Outcome - No |
| ---: | :---: | :---: |
| Exposed | a | b |
| Unexposed | c | d |

Probability of outcome in exposed $=\frac{a}{a+b}$

Odds Ratio: $\frac{\frac{a}{b}}{\frac{c}{d}}=\frac{a}{b} \times \frac{d}{c}=\frac{a d}{b c}$

Relative Risk: $\frac{\left(\frac{a}{a+b}\right)}{\left(\frac{c}{c+d}\right)}$

## In the beginning...

there were 2 by 2 tables:

|  | Controlled <br> Diabetes | Uncontrolled <br> Diabetes |
| ---: | :---: | :---: |
| Drug A | a | b |
| Placebo | c | d |

Probability of controlled diabetes with Drug $A=\frac{\boldsymbol{a}}{\boldsymbol{a}+\boldsymbol{b}}$

Odds Ratio: $\frac{\frac{a}{c}}{\frac{c}{d}}=\frac{a}{b} \times \frac{d}{c}=\frac{a d}{b c}$

Relative Risk: $\frac{\left(\frac{a}{a+b}\right)}{\left(\frac{c}{c+d}\right)}$

## OR versus RR

| Statistic | Evaluates |
| :--- | :--- |
| Relative Risk (aka Risk Ratio) | $\frac{\text { Probability of outcome in exposed }}{\text { Probability of outcome in unexposed }}$ |
| Odds Ratio | $\frac{\text { Odds of outcome in exposed }}{\text { Odds of outcome in unexposed }}$ |
| Odds | $\frac{\text { Probability of outcome }}{1-\text { Probability of outcome }}$ |

- RR is easier to interpret than OR
- But, the OR has better statistical properties
- OR of harm is inverse of OR of benefit
- RR of harm is not the inverse of $R R$ of benefit
- Much data in the literature is reported as OR


## Probability from RR

$$
R R=\frac{\text { probability in exposed }}{\text { probability in unexposed }}
$$

$\operatorname{prob}($ exposed $)=R R * \operatorname{prob}($ unexposed $)$
$\operatorname{prob}($ exposed $)=\frac{\downarrow}{\frac{\downarrow}{\text { prob (exposed) }}} \underset{\text { prob (tnexposed })}{ } \quad * \frac{\text { prob (mnexposed })}{}$

This requires that you are able to find the probability of unexposed in the journal article

## Probability from RR, example

- Example:
$-\mathrm{RR}=2.37$
- Probability in unexposed $=0.17$
- Probability in exposed $=2.37 * 0.17$

$$
\begin{aligned}
& =0.403 \\
& =40.3 \%
\end{aligned}
$$

over the entire study period

## Probability from RR, caveat

- If the RR is the result of a regression, it has been adjusted for covariates
- But, the probability in the unexposed will be unadjusted

- Therefore, your derived probability estimate will have some bias - so make sure you vary this in sensitivity analyses!


## RR are nice, but...

- OR are more likely to be reported in the literature than RR


## Probability from OR

- IF the outcome in the unexposed is rare ( $\leq 10 \%$ ), then you can assume that the OR approximates the RR
- If the outcome is not rare $\rightarrow$ advanced topic, do not proceed without consulting a statistician


## OR versus $\mathbf{R R}$



The relationship between risk ratio ( RR ) and odds ratio by incidence of the outcome.

## OR is a good measure of RR when the outcome is rare

## Calculating Probability from OR

- If outcome is rare, assume OR approximates RR
- Prob (exposed) = Rर́ * prob(unexposed)

OR
Example:
$\mathrm{OR}=1.57$
Prob. of outcome in unexposed: $8 \% \rightarrow$ rare

$$
\operatorname{prob}(\text { exposed })=1.57 * 0.08=12.56 \%
$$

|  | Outcome <br> -Yes | Outcome <br> - No |
| ---: | :---: | :---: |
| Exposed | 12 | 88 |
| Unexposed | 8 | 92 |

## Prob $_{\text {Unexposed }}$

- Whether you can assume the OR approximates RR depends on the probability of outcome in the unexposed
- Should be available in the paper
- If it is not - try going to the literature to find this value for a similar group of patients


## Probability from Odds

$$
\text { odds }=\frac{\text { probability }}{1-\text { probability }} \quad \text { probability }=\frac{o d d s}{1+o d d s}
$$

Odds of $1 / 7=$
Probability of 0.125

$$
\text { Probability }=\frac{1}{8}{ }_{7}=\frac{0.143}{1.143}=0.125
$$

## Probability from Stata, directly

■ "Margins" command

- logistic y i.x
- margins i.x
- Will give you predicted probabilities of $x$, given $\mathrm{y}=1$


## Converting to Probabilities?

| Statistic |  | Convert to probability? |
| :--- | :--- | :--- |
| $\checkmark$ | Probability/Risk <br> (aka Incidence Proportion) | n/a (use rates to convert the time period to which <br> they apply) |
| $\checkmark$ | Rate | Yes |
| $\checkmark$ | Odds | Yes |
| $\checkmark$ | Odds Ratio | Yes, if the outcome is rare $(\leq 10 \%)$ \& you have <br> probability in unexposed |
| $\checkmark$ | Relative Risk (aka Risk Ratio) | Yes, if you have the probability in the unexposed |
|  | Risk Difference (x-y=z) |  |
| Survival Curve |  |  |
|  | Mean |  |

## Risk Difference

- Risk in one group minus risk in the other
- Risk = probability
- Prob $_{\text {Drug A }}-$ Prob $_{\text {placebo }}=$ Risk Difference
- $0.84-0.17=0.67$


## Risk Difference, con't

- Prob $_{\text {treatment }}-$ Prob $_{\text {control }}=$ Risk Difference
- If the article gives you Risk Difference, it will often give you Prob ${ }_{\text {treatment }}$ or Prob $_{\text {control }}$
- If article gives you Prob $_{\text {treatment }}$, use that directly
- If article Prob $_{\text {control }}$, use that and the Risk Difference to derive Prob $_{\text {treatment }}$


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| $\checkmark$ | Relative Risk (aka Risk Ratio) | Yes, if you have the probability in the unexposed |

## Survival data and probabilities

- All previous probabilities were assumed to be constant throughout the model
(Don't have to be, but can be)
- Survival should NOT be assumed to be constant over time
- So, you will have multiple probabilities for "death" in your model - one for each time period of interest.


## Sources of survival data

- All-cause mortality (CDC)
- age- and sex-adjusted rates
- Disease-specific/Treatment-specific literature
- Probability of death at $t$
- Survival Curves


## Reported survival rates

## Table 3 Number-of doathe_and death rates, by age, race, and sex: United States, 2010-Con.

[Rates per 100,000 population in specified group. Rates are based on populations enumerated in the 2010 census as of April 1 ; see Technical Notes. Data for specified races other than white and black should be interpreted with-oution hecause of inconsistencies hatwoem-teporting race on death certificates and on censuses and surveys; see Technical Notes]

| Age (years) | All races |  |  | White ${ }^{1}$ |  |  | Black ${ }^{1}$ |  |  | American Indian or Alaska Native ${ }^{1,2}$ |  |  | Asian or Pacific Islander ${ }^{1,3}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Both sexes | Male | Female | Both sexes | Male | Female | Both sexes | Male | Female | Both sexes | Male | Female | Both sexes | Male | Female |
|  | Rate |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| All ages ${ }^{4}$ | 799.5 | 812.0 | 787.4 | 861.7 | 866.1 | 857.3 | 682.2 | 725.4 | 642.7 | 365.1 | 397.5 | 332.4 | 301.1 | 327.0 | 277.3 |
| Under 1 year ${ }^{5}$ | 623.4 | 680.2 | 564.0 | 537.2 | 584.3 | 488.0 | 1,102.1 | 1,206.5 | 994.4 | 455.3 | 542.5 | 366.4 | 389.3 | 434.4 | 341.8 |
| 1-4. . . . . . | 26.5 | 29.6 | 23.3 | 24.6 | 27.4 | 21.6 | 38.1 | 42.9 | 33.2 | 29.4 | 34.3 | 24.4 | 17.9 | 19.3 | 16.3 |
| 5-9. | 11.5 | 12.8 | 10.1 | 10.9 | 12.1 | 9.7 | 15.0 | 16.9 | 13.0 | 12.2 | 15.2 | * | 8.5 | 9.6 | 7.4 |
| 10-14 | 14.3 | 16.3 | 12.1 | 13.6 | 15.6 | 11.5 | 19.1 | 22.2 | 16.0 | 16.6 | 21.1 | 12.0 | 7.8 | 7.2 | 8.5 |
| 15-19 | 49.4 | 69.6 | 28.1 | 47.0 | 64.7 | 28.3 | 67.0 | 102.5 | 30.5 | 61.5 | 87.1 | 34.5 | 22.8 | 29.3 | 15.9 |
| 20-24 | 86.5 | 126.4 | 44.8 | 82.7 | 119.2 | 44.2 | 122.4 | 189.1 | 57.3 | 102.8 | 147.5 | 53.7 | 36.9 | 55.3 | 18.0 |
| 25-29 | 96.0 | 135.7 | 55.7 | 92.6 | 130.0 | 53.6 | 140.3 | 206.0 | 79.5 | 110.4 | 139.6 | 79.1 | 37.9 | 53.7 | 23.4 |
| 30-34 | 110.2 | 147.7 | 72.6 | 106.1 | 141.5 | 69.5 | 164.6 | 228.4 | 107.1 | 134.7 | 174.5 | 92.6 | 40.5 | 51.4 | 30.8 |
| 35-39 | 138.8 | 175.4 | 102.6 | 133.8 | 169.5 | 97.3 | 208.7 | 263.0 | 160.5 | 175.4 | 216.1 | 133.5 | 51.9 | 67.2 | 38.1 |
| 40-44 | 201.1 | 248.4 | 154.3 | 194.7 | 241.8 | 146.9 | 291.4 | 351.2 | 237.7 | 232.1 | 302.3 | 160.4 | 80.3 | 101.8 | 61.1 |
| 45-49 | 324.0 | 401.0 | 248.9 | 314.4 | 392.5 | 236.7 | 458.8 | 549.8 | 377.8 | 348.7 | 431.2 | 267.6 | 132.6 | 164.8 | 104.0 |
| 50-54 | 491.7 | 613.5 | 374.5 | 471.9 | 592.7 | 353.5 | 731.5 | 893.0 | 589.3 | 477.8 | 570.0 | 390.5 | 207.2 | 268.6 | 154.0 |
| 55-59 | 711.7 | 911.2 | 524.5 | 678.9 | 869.4 | 496.1 | 1,104.8 | 1,425.7 | 833.0 | 699.4 | 878.5 | 532.2 | 322.1 | 427.8 | 234.2 |
| 60-64 | 1,015.8 | 1,269.2 | 781.7 | 982.4 | 1,222.1 | 756.2 | 1,523.4 | 1,977.9 | 1,151.8 | 892.0 | 1,047.5 | 745.9 | 492.9 | 632.2 | 378.1 |
| 65-69 | 1,527.6 | 1,871.3 | 1,222.0 | 1,495.8 | 1,825.2 | 1,197.3 | 2,148.8 | 2,745.1 | 1,691.9 | 1,377.8 | 1,591.5 | 1,185.6 | 765.6 | 982.5 | 584.3 |
|  | 2,040.9 | 2,001.9 | 1,926.9 | 2,315.5 | 2,792.1 | 1,905.9 | 3,041.6 | 3,862.0 | 2,457.3 | 2,202.4 | 2,555.9 | 1,906.4 | 1,285.7 | 1,555.4 | 1,062.5 |
| 75-79. | 3,735.4 | 4,493.7 | 3,151.9 | 3,734.9 | 4,472.1 | 3,154.8 | 4,450.5 | 5,677.3 | 3,679.8 | 3,221.2 | 3,840.9 | 2,761.3 | 2,155.2 | 2,598.0 | 1,831.3 |
| 80-84 | 6,134.1 | 7,358.2 | 5,319.8 | 6,171.5 | 7,379.2 | 5,351.7 | 6,710.4 | 8,414.7 | 5,809.8 | 4,811.0 | 5,489.7 | 4,357.2 | 3,895.1 | 4,791.6 | 3,316.8 |
| 85 and over | 13.934 .3 | 15.414 .3 | 13,219.2 | 14,147.6 | 15,640.3 | 13,419.3 | 13,187.2 | 14,715.3 | 12,589.9 | 9,615.3 | 10,268.1 | 9,277.9 | 9,418.1 | 10,824.5 | 8,590.1 |

## Survival Rate $\rightarrow$ Probability

| Age range | CDC <br> numbers |
| :--- | :--- |
| $75-79$ | 4493.7 |
| $80-84$ | 7358.2 |
| $85+$ | 15414.3 |


| Rate | Prob. of death |
| :--- | :---: |
| $4493.7 / 100,000=0.44937$ | $4.39 \%$ |
| $7358.2 / 100,000=.073582$ | $7.09 \%$ |
| $15414.3 / 100,000=0.154143$ | $14.29 \%$ |

$$
\text { Probability }=1-e^{(-r t)}
$$

| Cycle | Age | Prob. of death |
| :--- | :--- | :--- |
| 0 | 75 | .0439 |
| 1 | 76 | .0439 |
| 2 | 77 | .0439 |
| 3 | 78 | .0439 |
| 4 | 79 | .0439 |
| 5 | 80 | .0709 |
| 6 | 81 | .0709 |
| 7 | 82 | .0709 |
| 8 | 83 | .0709 |
| 9 | 84 | .0709 |
| 10 | 85 | .1429 |
| 11 | 86 | .1429 |
| . | . | . |
| . | . | . |

## Disease-Specific Survival Data

■ Kaplan-Meier Curve

- Unadjusted
- RCT data

■ Cox Proportional Hazards Curve

- Adjusted
- observational data


## Survival Data from Curves

Figure 4
Kaplan-Meier curves for the secondary endpoint of hospital admission
Estimates of survival free from hospital admission for cardiac reasons. Censored patients are indicated by dots.


## Converting to Probabilities?

| Outcome |  | Convert to probability? |
| :--- | :--- | :--- |
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| $\checkmark$ | Odds Ratio | Yes, if the outcome is rare ( $\leq 10 \%)$ \& you have prob. in <br> unexposed |
| $\checkmark$ | Relative Risk (aka Risk Ratio) | Yes, if you have the probability in the unexposed |
| $\checkmark$ | Risk Difference (x-y= z) | Most likely, because they will give you x or y in addition to <br> z |
| $\checkmark$ | Survival Curve | Yes, but remember they are conditional and may change <br> with each time period |
|  | Mean |  |

## Deriving probability from mean (continuous distribution)

- 1) Need a validated way to generate a binary variable from a continuous distribution -- threshold
$-\mathrm{HbAlc}<7=$ controlled diabetes
- 2) Need an estimate of variation around the mean (SD, variance) or median (IQR, range)
- Involve a statistician!


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| $\checkmark$ | Survival Curve | Yes, but remember they are conditional and may change <br> with each time period |
| $\checkmark$ | Mean | Yes, if you have estimate of variation |

## Estimates of variation

- You will still need to derive estimates of variation around your derived point estimate of probability
- Necessary for sensitivity analyses
- Advanced Topic


## Quality of the literature

■ THE QUALITY OF THE LITERATURE MATTERS GREATLY!!


- Preferences for literature-based inputs:

1. These two treatments studied in a head-to-head RCT
2. a) Drug compared to placebo in RCT, and
b) Diet/Exercise/Telehealth compared to placebo in another RCT, and
c) these two RCTs enrolled similar patients

## Summary

- Need to transform reported data to probabilities for use in a decision model
- Easiest: Rate, OR if outcome $<10 \%$, RR, survival data
- More difficult, but possible: Continuous data with estimate of variation
- Advanced topics: OR when outcome $>10 \%$, mean difference, standardized mean difference
- Probs. apply to particular length of time - To change the length of time to which a probability applies:
- Probability $\rightarrow$ rate $\rightarrow$ probability


## References

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## Questions?

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